

# Year 11 Higher Term 1 – Knowledge Organiser

## Circle Theorems

You need to remember all the keywords in here to be able to describe them -

**KEYWORDS**  
Tangent, Chord, Circumference, Diameter, Angle, Cyclic, Radius

## Simultaneous Equations the harder ones!!

$$x^2 + y^2 = 25 \quad (1)$$

$$y = x + 1 \quad (2)$$

**Factorise**  
 $(x + 4)(x - 3) = 0$

**Solve**  
 $x + 4 = 0 \quad x - 3 = 0$   
 $x = -4 \quad x = 3$

**Sub (2) into (1)**  
 $x^2 + (x + 1)^2 = 25$   
 $x^2 + x^2 + 2x + 1 = 25$   
 $2x^2 + 2x + 1 = 25$   
 $2x^2 + 2x - 24 = 0$

**Divide equation by 2**  
 $x^2 + x - 12 = 0$

**Sub x values into (2) to find y**  
 $y = -4 + 1 \quad y = 3 + 1$   
 $y = -3 \quad y = 4$

**Answers**  
 $x = -4, y = -3$   
 $x = 3, y = 4$

## Set Notation

– {This is where we use those wiggly brackets}

**Set Notation**

**List them!**  
{1,3,5,7,9,11,13}

**Describe them!**  
{the odd natural numbers greater than 0 and less than 14}

**More formal notation (set-builder notation)**  
 $\{x \in \mathbb{N} \mid 0 < x < 14, x \text{ is odd}\}$

all the numbers that are in the natural numbers such that

These could come up with Venn diagrams as-well.

**Keywords**  
Set Notation

## Algebraic Fractions ...

3 things to be able to do

1. Simplify – factorise top and bottom and cancel out like terms and brackets
2. Manipulate - +, x, /, - Process the fractions the same way you would numerical fractions
3. Solve – Find the value for x.... these are the hardest, you will need to move around the algebra from side to side, then prob have to factorise aswell at the end.....

## Iteration

Repeat- repeat - repeat

**Fixed Point Iteration**

$$x^2 - x - 1 = 0$$

$$x_{n+1} = 1 + \frac{1}{x_n}$$

Pick  $x_1 = 2$

$$x_2 = 1 + \frac{1}{2} = 1.5$$

$$x_3 = 1 + \frac{1}{1.5} = 1.666$$

$$x_4 = 1 + \frac{1}{1.666} = 1.6$$

Remember to use your ans button on your calculator to help you out here.

**Keywords** – Iteration; converging, diverging, oscillating sequences

## Vectors

– You are going to have to.....

1. Manipulate - +, x, /, - them
2. Draw them
3. Use them in geometry
4. Find the magnitude (length) of them.

1.

2.

3.

4.

If  $a = \begin{pmatrix} x \\ y \end{pmatrix}$  then the magnitude  $|a| = \sqrt{x^2 + y^2}$  [by Pythagoras Theorem]

**revision maths**

Note – parallel vectors are a scalar product of each other.

**KEYWORDS**  
Vector, Magnitude, Parallel, perpendicular, Direction

## Circles and their Tangents

Here you need to find the equation of the tangent, remember it is perpendicular to the radius.

**Circle Problems**

1. Find the equation of the tangent at the point  $A(3, -2)$  on the circle  $x^2 + y^2 = 13$

Solution: Centre is  $(0, 0)$ . Sketch!

Gradient of radius,

$$m_1 = \frac{y_2 - y_1}{x_2 - x_1} \Rightarrow m_1 = \frac{-2 - 0}{3 - 0} = -\frac{2}{3}$$

⇒ Gradient of tangent,

$$m_2 = -\frac{1}{m_1} \Rightarrow m = \frac{3}{2}$$

$y = mx + c \Rightarrow -2 = \frac{3}{2}(3) + c \Rightarrow -\frac{13}{2} = c$

⇒ Equation of tangent is  $y = \frac{3}{2}x - \frac{13}{2}$  or  $2y - 3x + 13 = 0$

### KEYWORDS

Tangent, Radius, Gradient, Co-ordinates, Perpendicular

**Completing the Square...** this has lots of uses!!!

- Shows the transformation of  $y=x^2$
- Shows the turning point of the graph
- Gives the line of symmetry of the graph.
- when solved gives the points of intersection with the X axis.

How cool is that!!!

- [ 2. The turning point of the one on the right is  $(2, 5)$
3. Making the line of symmetry  $x=2$  ]

How to do it...

### Completing the Square

$$x^2 - 4x + 9 = 0 \text{ (original equation)}$$

$$x^2 - 4x = -9 \text{ (subtract 9 from both sides)}$$

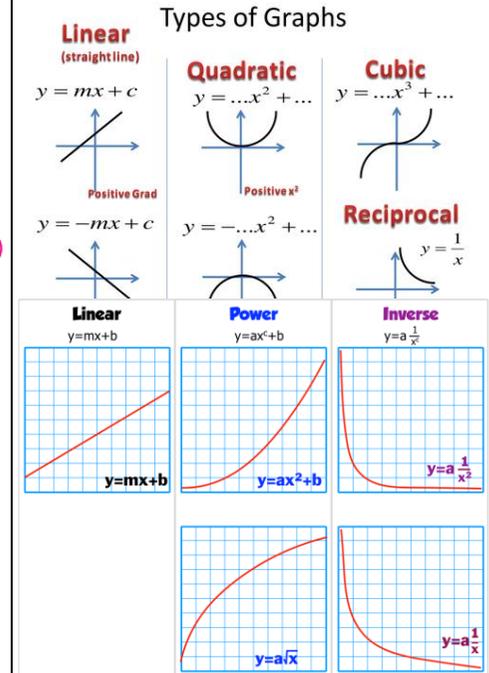
$$x^2 - 4x + 4 = 5 \text{ (take half of } b, \text{ then square it and add that value to both sides of the equation)}$$

$$(x - 2)^2 = 5 \text{ (break your perfect square into its binomials, made up of } x, \text{ the sign in front of } b, \text{ and the square root of your new } c)$$

$$x - 2 = \sqrt{5} \text{ or } -\sqrt{5} \text{ (take the square root of both sides)}$$

$$x = 2 + \sqrt{5} \text{ or } 2 - \sqrt{5} \text{ (add 2 to both sides)}$$

## Graph Recognition



## Plotting Graphs

Any graph can be plotted the same way...

- Draw a table of values for  $x$
- Substitute these values into the graph you have been given, to find values for  $y$ .
- Plot on an axis, if you are lucky they will provide an axis, if not then make sure your scale is accurate.

## Algebraic Proof

**WHY OH WHY DO WE DO THIS.....I hear you asking..**

**Well it can be used to prove pretty much everything in maths.**

Processes:

- Manipulate the algebra they have given you and factorise it to prove what they have asked

2. You may need to allocate your own algebra...

Remember -

$n, n+1, n+2, n+3 \dots$  Are consecutive numbers.

$2n$  is an even number

$2n-1$  is always an odd number.

## Algebra Proof Solution

- Follow the steps.
- Justify the steps.
- $x + y = 60$
- Given
- $x = 5$
- Given
- $5 + y = 60$
- Substitution
- Property of Equality
- $y = 55$
- Subtraction
- Property of Equality